

# Overhead Considerations in Real-time Energy Harvesting Systems

Hussein El Ghor<sup>1</sup> and Maryline Chetto<sup>2</sup>

<sup>1</sup>*Lebanese University, University Institute of Technology, B.P. 813, Saida, Lebanon*

<sup>2</sup>*IRCCyN Research Institute, University of Nantes 1, Rue de la Noe, F-44321 Nantes, France  
hussein.ghor@ul.edu.lb, maryline.chetto@univ-nantes.fr*

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**Abstract:** The effectiveness of a real-time scheduling algorithm depends on both its ability to schedule feasible task sets and its runtime overhead. In this paper, we investigate overheads incurred by a scheduler dedicated to embedded systems that are powered by renewable energy. We specifically focus on the overhead cost of an EDF-based scheduler known as ED-H. We analyze the number of tasks factor that can possibly affect the resulting performance of ED-H. The simulation experiments demonstrate that the implementation costs of ED-H remain acceptable so as to make it a practicable scheduler.

## 1 INTRODUCTION

The overhead of an operating system represents the time lost in handling all kernel mechanisms such as context-switching and task scheduling management. Context-switching overhead is the time needed to preempt a task, save its context, load the context of another task and resume that task. This overhead is only incurred in a preemptive environment. A context switch is forced only when the active task ceases to be the highest priority one. For any scheduling algorithm, the overhead incurred by its implementation results from the computational complexity of the algorithm that is used to select the future active task. In most of papers found in the literature, it is assumed that the overhead cost is negligible. This hypothesis is realistic for most of traditional schedulers that do not perform on-line computations. They just amount to order lists of tasks according to a given priority rule and dispatch the highest priority task at scheduling points. Whatever the priority assignment rule, the overhead is limited. Most of priority driven schedulers are work-conserving in that sense they never let the processor idle whenever at least one task is pending for execution (Iiu, 2000). Consequently, no computation is involved in determining when the processor should be active.

Recently (Chetto, 2014), we addressed the scheduling problem that arises in a uniprocessor platform that is powered by a renewable energy storage unit and uses a recharging device such as photovoltaic

cells (Kansal and Hsu, 2006). We proposed a dynamic priority scheduling algorithm called ED-H. ED-H is based on the EDF (Earliest Deadline First) dynamic priority assignment rule (Liu and Layland, 1973). ED-H is a generalization of a scheduling heuristic called EDeg that we introduced in 2011 (Ghor et al., 2011). ED-H considers a set of deadline constrained tasks including periodic tasks whose characteristics are well known at design time. ED-H is a clairvoyant scheduler that requires to know in advance both the energy source profile and characteristics of the tasks (arrival time, computation time and energy requirement).

The ED-H scheduler involves overhead due to specific on-line computations which are absent in the classical EDF scheduler that greedily consumes energy. ED-H requires the online computation of two data respectively called slack time and slack energy in order to build the schedule at run time. The overhead of the ED-H scheduler clearly depends on both the computational complexity for slack time and slack energy and the frequency of these computations.

In (Chetto, 2014), we proved that ED-H is optimal. But gaining in performance generally means losing in cost. Consequently, this paper aims to show that the gain in performance in comparison with classical EDF scheduler turns out to be higher than the actual overhead cost.

The rest of the paper is organized as follows: We first introduce the model and terminology in Section 2. Section 3 describes the necessary background for ED-H including slack time and slack energy concepts.

Overhead evaluation is described in Section 4. Section 5 is concerned with experimental results. Finally, we conclude the paper in Section 6.

## 2 MODEL AND TERMINOLOGY

### 2.1 Task Set

We consider a real-time system that is composed of  $n$  periodic tasks. A task  $\tau_i$  is described by a Worst Case Execution Time (WCET) of  $C_i$  time units and relative deadline  $D_i$ . We assume that  $0 \leq C_i \leq D_i \leq T_i$  for each  $1 \leq i \leq n$ . Timing values are generally expressed in seconds. A periodic task  $\tau_i$  makes its initial request at time 0 and its subsequent requests at times  $k.T_i$ ,  $k = 1, 2, \dots$  called release times. The least common multiple of  $\{T_1, T_2, \dots, T_n\}$  (called the hyperperiod) is denoted by  $T_{LCM}$ . Each request of  $\tau_i$  requires a Worst Case Energy Consumption (WCEC) of  $E_i$  energy units. We define the processor utilization as  $U_p = \sum_{i=1}^n \frac{C_i}{T_i}$  and the energy utilization as  $U_e = \sum_{i=1}^n \frac{E_i}{T_i}$ .

### 2.2 Energy Model

We concentrate on the harvested energy since it can incorporate all losses caused by power conversion and charging process. We assume that the energy source is uncontrolled but predictable: we cannot control it but its behavior may be modeled to predict the expected availability at a given time within some error margin. The energy source module harvests the energy from its ambient environment and then converts it into electrical energy at power  $P_r(t)$  where  $P_r(t)$  is called the WCCR (Worst Case Charging Rate).

The harvested energy is stored in an energy storage unit with capacity  $E$ . The energy level has to remain between two boundaries  $E_{min}$  and  $E_{max}$  with  $E = E_{max} - E_{min}$ . The stored energy may be used at any time later and does not leak any energy over time. If the storage is fully charged, and we continue to charge it, energy is wasted. In contrast, if the storage is fully discharged, no job can be executed.

## 3 BACKGROUND MATERIALS

In this section we describe the ED-H scheduling algorithm that has been proposed in (Chetto, 2014). The idea behind ED-H is to order the jobs according to the EDF rule since the jobs issued from the periodic tasks have hard deadlines. Executing them in accordance

with their relative urgency appears to be the best approach even if they are not systematically executed as soon as possible due to possible energy shortage.

The difference between ED-H and classical EDF is to decide when to execute a job and when to let the processor idle. Before authorizing any job to execute, the energy level of the storage must be sufficient so that all future occurring jobs execute timely with no energy starvation, considering their timing and energy requirements and the replenishment rate of the storage unit. In our model, any job consumes energy with instantaneous power that fluctuates along its execution.

Before starting the execution of any job, it must be verified that the energy will be available to execute it until completion with no energy starvation.

If this condition does not hold, the processor has to idle during a certain time interval. The recharging process terminates when either the energy storage unit has fully replenished or one job absolutely needs to start execution so that all deadlines can be met.

The ED-H algorithm uses three major data respectively denoted by  $E(t)$ ,  $Slack\_energy(t)$  and  $Slack\_time(t)$  where  $t$  is the current time.  $E(t)$  refers to the amount of energy that is currently stored at time  $t$ .  $Slack\_energy(t)$  and  $Slack\_time(t)$  are respectively the slack energy and the slack time of the system at time  $t$  (as defined later in this article). Let  $PENDING(t)$  be a boolean which equals true whenever there is at least one job in the ready list queue at time  $t$ . Function  $wait()$  puts the processor in the sleep mode. Function  $execute()$  puts the processor in the active mode and starts executing the highest priority job in the ready list.

ED-H checks the ready list queue at every current time  $t$  since it is a preemptive scheduler. The processor idles if the ready list is empty. Else ED-H selects the highest priority job for execution. Nonetheless, ED-H authorizes the execution of the job only if the slack energy has a positive value. Otherwise, the processor idles. The question is: for how long time? ED-H answers this question by computing the slack time of the system. And the processor will be let inactive until the next time instant where either the energy storage unit fully replenishes or there is no more slack time. Let us note that whenever the processor does not execute any job, the slack time linearly decreases with time. ED-H also tests whether  $E(t) > E_{min}$  where  $E_{min}$  refers to the threshold for the level of the energy storage unit.

**Output:** The ED-H schedule.

```

1: while (1) do
2:   while PENDING(t)=true do
3:     while ( $E(t) > E_{min}$  and  $Slack\_energy(t) > 0$ ) do
4:       execute()
5:     end while
6:     while ( $E(t) < E_{max}$  and  $Slack\_time(t) > 0$ ) do
7:       wait()
8:     end while
9:   end while
10:  while PENDING=false do
11:    wait()
12:  end while
13: end while

```

### 3.1 Slack Time Computation

Slack time is a well known concept used in the conventional literature about real-time scheduling. By definition, the *slack time* of a hard deadline task set at current time  $t$  is the length of the longest interval starting at  $t$  during which the processor may be idle continuously while still satisfying all the timing constraints. The slack time of a periodic task set at a given time instant can be obtained on-line by computing the dynamic EDL schedule. Details of computation are given in (Silly-Chetto, 1999).

**Proposition 1.** *The time complexity for computing the slack time at run time is  $O(K.n)$  with  $n$  the number of periodic tasks,  $K$  equal to  $\lceil R/p \rceil$ ,  $R$  and  $p$  respectively the longest deadline and the shortest period of tasks.*

### 3.2 Slack Energy Computation

The *slack energy* of the periodic task set at current time  $t$ , is defined as the maximum amount of energy that can be consumed from  $t$  continuously while still satisfying all the timing constraints. The slack energy at time  $t$  is computed only when there is at least one job, say  $J_j$  which will be released after  $t$  and has a deadline  $d_j$  that is less than or equal to that of the highest priority job, ready at  $t$ . The slack energy of the system is determined by the minimum slack energy of all the jobs.

Then the slack energy of job  $J_j$  at time  $t$  will be given by:

$$Slack\_energy(J_j, t) = E(t) + \int_t^{d_j} P_r(k) dk - A_j \quad (1)$$

Where  $A_j$  is the energy demand within  $[t, d_j)$  required by the periodic jobs ready to be processed between  $t$  and  $d_j$ .

$$A_j = \sum_{d_k \leq d_j} E_k \quad (2)$$

Consequently, the slack energy of the system at time  $t$  is determined by:

$$Slack\_energy(t) = \min(Slack\_energy(J_j, t)) \quad (3)$$

**Proposition 2.** *The time complexity for computing the slack energy is  $O(K.n)$  with  $n$  the number of periodic tasks,  $K$  equal to  $\lceil R/p \rceil$ ,  $R$  and  $p$  respectively the longest deadline and the shortest period of tasks.*

## 4 OVERHEAD EVALUATION

The overhead of ED-H depends on the complexity for computing slack time and slack energy and the number of times we are obliged to compute these two quantities. In order to compute the total overhead incurred by slack time and slack energy computations, we have to evaluate:

- the overhead for one slack time computation,
- the overhead for one slack energy computation,
- the number of slack time computations in a reference interval,
- the number of slack energy computations in a reference interval.

The *global overhead* refers to the total overhead due to slack time computations plus the total overhead due to slack energy computations.

### 4.1 Illustrative Example

Let us illustrate the overhead measurement for slack time computation, one slack energy computation and finally the global overhead. We consider a periodic task set  $\Gamma$  composed of three periodic tasks  $\tau_i$  with  $\tau_i = (C_i, D_i, T_i, E_i)$ . Let  $\tau_1 = (1, 5, 6, 12)$ ,  $\tau_2 = (2, 8, 10, 15)$  and  $\tau_3 = (4, 11, 15, 22)$ . We assume that the level in the storage unit at time 0 is  $E(0) = 25$ . It equals the capacity of the energy storage unit. The environmental power varies over time as described in table 1. Tasks in  $\Gamma$  are first scheduled according to the EDS rule (i.e. executed as soon as possible) until  $t = 10$  where  $E(10) = 13$ . At  $t = 10$ ,  $\tau_2$  is the highest priority task. The slack energy of the system is then computed from all jobs released after  $t = 10$  with absolute deadline less than or equal to the absolute deadline of  $\tau_2$  equal to 18.

Table 1: Values of  $P_r(t)$ .

Interval of time	[0, 1]	[1, 2]	[2, 3]	[3, 4]	[4, 5]	[5, 6]	[6, 7]	[7, 8]	[8, 9]	[9, 10]
$P_r(t)$	5	3	4	6	2	4	7	8	4	6
Interval of time	[10, 11]	[11, 12]	[12, 13]	[13, 14]	[14, 15]	[15, 16]	[16, 17]	[17, 18]	[18, 19]	[19, 20]
$P_r(t)$	3	7	8	4	2	5	4	7	3	5
Interval of time	[20, 21]	[21, 22]	[22, 23]	[23, 24]	[24, 25]	[25, 26]	[26, 27]	[27, 28]	[28, 29]	[29, 30]
$P_r(t)$	4	6	7	3	7	8	3	4	5	6

$$\text{Slack\_energy}(J_1, 10) = E(10) + \int_{10}^{17} P_r dt - E_1 = 34 \quad (4)$$

The overhead incurred by the slack energy computation is 7 defined as the number of arithmetic operations implemented in that computation.

$$\begin{aligned} \text{Slack\_energy}(J_2, 10) &= E(10) + \int_{10}^{18} P_r dt - (E_1 + E_2) \\ &= 26 \end{aligned} \quad (5)$$

Thus, the overhead for one computation of the slack energy is 8. At time  $t = 15$ , the slack energy needs to be computed again. This generates an overhead equal to 19 operations. At  $t = 18$ ,  $\tau_1$  is the highest priority task ready for execution and  $E(18) = 4$ . Nevertheless, there is no sufficient energy in the energy storage for starting execution of  $\tau_1$ . The processor stays inactive as long as the energy storage has not filled completely and the latest start time has not been attained. This presupposes to compute the slack time of the system. The static idle time vector and the static deadline vector are assumed to be available with no computation since these values are computed off-line. We have  $\mathcal{K} = (0, 5, 8, 11, 17, 18, 23, 26, 28, 29)$  and  $\mathcal{D} = (3, 0, 0, 4, 0, 2, 0, 0, 1, 1)$ .

The dynamic *EDL* schedule for the interval  $[18, 30]$  is obtained from the dynamic deadline vector  $\mathcal{K}(18) = (18, 23, 26, 28, 29)$  and the dynamic idle time vector  $\mathcal{D}(18) = (4, 2, 0, 1, 1)$ . Three on-line computations are performed for obtaining  $\mathcal{D}(18)$ . Consequently, the overhead generated by this slack time evaluation amounts to 3 operations. The slack time at  $t = 18$  equals 4 time units. At  $t = 22$ , the energy level is  $E(22) = 22$  energy units. Instances are executed according to *EDS* until  $t = 24$  where the battery storage unit becomes empty, needs to recharge thus involving computation of the slack time with overhead equal to 3. Scheduling continues until the end of the hyperperiod where  $E(30) = 10$ .

From the observation of ED-H along one hyperperiod, we conclude that:

- The number of slack time computations equals 2,
- The number of slack energy computations equals 2,

- The total overhead due to slack energy computation equals 34,
- The total overhead due to slack time computation equals 6,
- Global overhead given by the total overhead incurred by slack time computations and slack energy computations equals 40, exactly  $34 + 6$ .

Consequently, the overhead cost per job amounts to 4 basic operations since 10 jobs occur within every hyperperiod.

## 5 EXPERIMENTAL RESULTS

In this section, we evaluate the overhead of the ED-H scheduler. We assume an energy source with constant power  $P_r$ . We have developed a discrete event-driven simulator in C. We report here an experiment to compare the overhead by varying the number of tasks. For a specific processor utilization setting, we repeat experiments for 50 periodic task sets. We report the experiments for task sets with high energy utilization and low energy utilization successively.

### 5.1 Task Sets with Low Energy Utilization

Let us assume that the normalized energy utilization  $U_e/P_r = 0.3$ . Consequently, the average consumption power of the tasks is about 30% of the harvested power. In this experiment, the time overhead is evaluated by varying the number of periodic tasks. Time overhead is defined as the number of times where we compute either the slack time or the slack energy relative to the total number of instances.

The number of slack time and slack energy computations is clearly not dependent on the number of tasks. However, the the number of overhead computations incurred by every computation of either the slack time or the slack energy linearly increases as the number of tasks increases. But when computing the time overhead, we have to divide the number of overhead computations by total number of instances.

Consequently, time overhead decreases upon increasing the number of tasks.

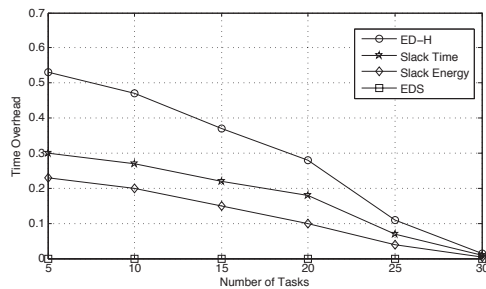


Figure 1: Time overhead by varying the number of tasks for low energy utilization.

Figure 1 shows that the time overhead decreases as  $n$  increases. Thus the overhead cost (about 0.15) is still in the acceptable margin and consequently it will not affect the performance gain of ED-H.

## 5.2 Task Sets with High Energy Utilization

We consider periodic task sets with normalized energy utilization  $U_e/P_r = 0.9$ .

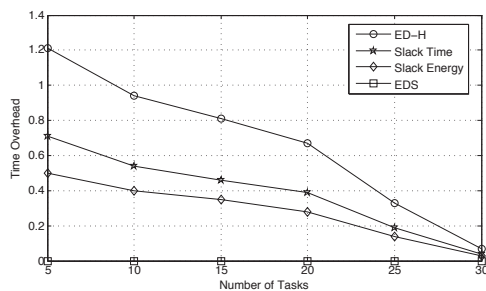


Figure 2: Time overhead by varying the number of tasks for high energy utilization.

Figure 2 shows that the overhead cost decreases as the number of tasks increases. If  $n$  increases with  $U_e/P_r$  keeping constant, the overall overhead cost due to slack energy computations decreases while the number of these computations remains constant.

In summary, the overhead increases by about 29% from low energy utilization to high energy utilization. Hence, the maximum overall overhead cost will be about 0.22, which is also still in the acceptable margin.

## 6 CONCLUSION

Traditional real-time schedulers behave poorly because they greedily consume the energy by execut-

ing systematically the tasks as soon as possible. Very recently, we presented the framework of a new mono-processor preemptive scheduling algorithm, namely ED-H. ED-H jointly handles constraints from both energy and time domain. For this purpose, we introduced the concept of slack energy that guarantees the absence of energy starvation for every task as long as the application is feasible.

In this paper, we presented the overhead cost of ED-H through a detailed simulation by varying the number of tasks. We explored specifically the time lost to compute at run time two key data, namely slack time and slack energy. Our interrogation has concerned the number of such computations on a reference interval given by the hyperperiod of the periodic tasks as well as the complexity of such computations.

The simulation study evaluated the impact of overheads on the relative performance of different scheduling strategies including EDF, the classical real-time scheduler which does not involve specific computations at run time. So in a hard real-time system where all the tasks must imperatively meet their timing requirements, it is of practical interest to prove that the gain in performance is higher than the incurred cost. To investigate the time overhead incurred by the schedulers under different application profiles, we made vary the number of tasks. The highest overhead cost is obtained under high energy utilization. Still, this value is acceptable and will not affect the performance of ED-H.

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